Waves in pre-stressed immersed plates and tubes: Application to ultrasound elastography of thin-walled soft materials

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Abstract

It is a great challenge to be able to measure the *in vivo* mechanical properties of thin-walled biological soft tissues such as mitral valve, artery and bladder. Here we investigate the properties of guided waves in immersed pre-stressed plates and tubes, and show that they can address this challenge. To this end, we carry out both (i) a theoretical analysis based on incremental wave motion in finite deformation theory and (ii) finite element simulations. Our analysis leads to a novel method based on the ultrasound elastography to image the elastic properties of pre-stressed thin-walled soft tissues and artificial soft materials in a non-destructive and non-invasive manner. To validate the theoretical measurements, we perform (iii) experiments on polyvinyl alcohol cryogel phantoms immersed in water.



(a) Curve-fitting of dispersion curves to experimental data for guided waves in a plate in plane strain with 0%, 8% and 18% stretch.

(b) Uni-axial (destructive) testing.

References

 G.-Y. Li, Q. He, R. Mangan, G. Xu, C. Mo, J. Luo, M. Destrade, Y. Cao, Guided waves in pre-stressed hyperelastic plates and tubes: Application to the ultrasound elastography of thin-walled soft materials, *Journal of the Mechanics and Physics of Solids*, in press, 2017. DOI: j.jmps.2017.02.008